



Magnetic order of YNi₄Si-type TbNi₄Si

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ABSTRACT

Magnetic measurements and neutron powder diffraction investigation of the magnetic structure of the YNi₄Si-type TbNi₄Si compound are presented. The magnetocaloric effect of TbNi₄Si is calculated in terms of the isothermal magnetic entropy change and it reaches the maximum value of -6.3 J/kg K for a field change of 0 – 50 kOe near T_C of ~ 37 K.

Below ~ 37 K and in a zero applied magnetic field, TbNi₄Si exhibits a commensurate b -axis collinear ferromagnetic ordering with the **Cmm'm** magnetic space group. At 1.5 K, the terbium magnetic moment reaches the value of $8.66(6)$ μ_B .

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1. Introduction

Recently, the orthorhombic derivative of the CaCu₅-type structure namely the YNi₄Si-type RNi₄Si compounds (R=Y, La–Ce, Sm, Gd–Ho) was reported [1]. Perhaps, the orthorhombic distortion of initial CaCu₅-type compounds is a prospective route for optimization of their magnetic and hydrogen storage properties [2–4]. Furthermore, the modification of the type structure of rare earth compounds via solid solution is useful method for the improvement of their magnetocaloric properties as clearly shown for the Gd₅Si₂Ge₂-based and LaCo₁₃-based solid solutions [5–7].

The initial CaCu₅-type TbNi₅ shows ferromagnetic ordering below $T_C \sim 26$ K with isothermal magnetic entropy change -11.5 J/kg K for a field change of 0 – 5 T [8]. In the zero applied field, TbNi₅ has a modulated ferromagnetic structure that is the superposition of the collinear ferromagnet with $\mathbf{K}_1=[0, 0, 0]$ and transverse spin wave with $\mathbf{K}_2=[0, 0, 0.018]$ in the basal plane. Two spontaneous transitions were observed in the TbNi₅ single crystal. At $T_C=24$ K, a second-order transition from the paramagnetic state to the incommensurate structure occurs. This is followed by a transition from the incommensurate structure to the lock-in type structure at $T_{SR}=10$ K. At 2 K an external magnetic field of 0.4 T is strong enough (when H is parallel to the c -axis) to induce a transition to a collinear ferromagnetic structure, which remains stable even when the external field is switched off [9].

One can speculate that the orthorhombic distortion achieved through the elemental substitution will influence the magnetic properties of the initial CaCu₅-type phases. This work aims to understand such changes in the YNi₄Si-type TbNi₄Si compound, an orthorhombic derivative of the original CaCu₅-type TbNi₅ phase, through the magnetic measurements and neutron powder diffraction.

2. Material and methods

The TbNi₄Si sample was prepared by arc melting of the stoichiometric amounts of Tb (99.9 wt%), Ni (99.95 wt%) and Si (99.99 wt%). The sample was annealed at 1070 K for 200 h in an argon-filled and sealed quartz tube and subsequently quenched in ice-cold water. The structure, purity and composition of the polycrystalline sample were evaluated using powder X-ray diffraction (XRD) and electron microprobe analysis. The X-ray data were obtained on a Rigaku D/MAX-2500 diffractometer (CuK _{α} radiation, $2\theta=10$ – 80 deg, step 0.02 deg, 1 s/step). An INCA-Energy-350 X-ray EDS spectrometer (Oxford Instruments) on the Jeol JSM-6480LV scanning electron microscope (20 kV accelerating voltage, beam current 0.7 nA and beam diameter 50 μ m) was employed to perform the microprobe analyses of the sample. Signals from three points were averaged and estimated standard deviations were 1 at % for Tb (measured by L-series lines), 1 at% for Ni and 1 at% for Si (measured by K-series lines).

DC magnetization of the polycrystalline TbNi₄Si sample (mass ~ 0.01 g) was measured on a commercial MPMS SQUID magnetometer (Quantum Design) in the temperatures range of

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5–300 K with an applied magnetic field of 100 Oe in the zero-field-cooled and field-cooled modes. The isothermal saturation magnetization was measured for the magnetic field change from 0 till 50 kOe and for the temperature range 10–60 K with a 5 K step.

Neutron diffraction experiments were carried out at the high flux reactor of the Institut Laue Langevin (Grenoble, France). The data were collected in a zero magnetic field on the two-axis D1B powder diffractometer equipped with a 1300 cell curved detector spanning the 2θ range of 130 deg [10]. The temperature ranges were 198–64 K with a step of ~ 10 K and 64–1.5 K with a step of ~ 5 K. The neutron wavelength of 2.52 Å was selected by the (002) reflection of a pyrolytic graphite monochromator and the 2θ step was 0.1 deg.

3. Theory/calculation

The unit cell data were derived from the powder XRD using the Rietan program [11,12] in the isotropic approximation at room temperature. The paramagnetic susceptibility was fitted to the Curie–Weiss law, the effective magnetic moment and paramagnetic Curie temperature were obtained from the fit [13]. Magnetocaloric effect (MCE) was calculated in terms of the isothermal magnetic entropy change, ΔS_{mag} , using the magnetization vs. field data obtained near the magnetic transition and employing the thermodynamic Maxwell equations [14]. The neutron diffraction data were refined with the FULLPROF program [15]. The “colorless” space groups and “black-white” magnetic space group [16–18] were used for the analysis of neutron diffraction data.

4. Results

4.1. Crystal structure

Both the microprobe and X-ray powder analyses showed that TbNi₄Si is a single-phase sample. The microprobe analysis yielded the Tb₁₆₍₁₎Ni₆₈₍₁₎Si₁₆₍₁₎ composition, and the X-ray powder analysis confirmed the YNi₄Si-type structure with the *Cmmm* space group. The refined lattice parameters were $a=0.50577(2)$ nm, $b=0.82131(3)$ nm, $c=0.39484(1)$ nm, $V=0.16401(4)$ nm³ and $b/(3^{1/2} \cdot a)=0.93755(3)$ and the atomic sites were Tb1 (2a) [0, 0, 0], Ni1 (4i)

[0, 0.3453(5), 0], Ni2 (4f) [1/4, 1/4, 1/2] and Si (2c) [0, 1/2, 1/2], $R_F=4.9\%$. The atomic positions for the Tb 2a site in the *Cmmm* space group with the corresponding symmetry operators are given in Table 1.

4.2. Magnetic properties and magnetocaloric effect

The zero-field-cooled (ZFC) and field-cooled (FC) magnetization data recorded during heating in 100 Oe are shown in Fig. 1a. The FC data are indicative of a typical ferromagnet, while the ZFC data suggest presence of weak competing antiferromagnetic

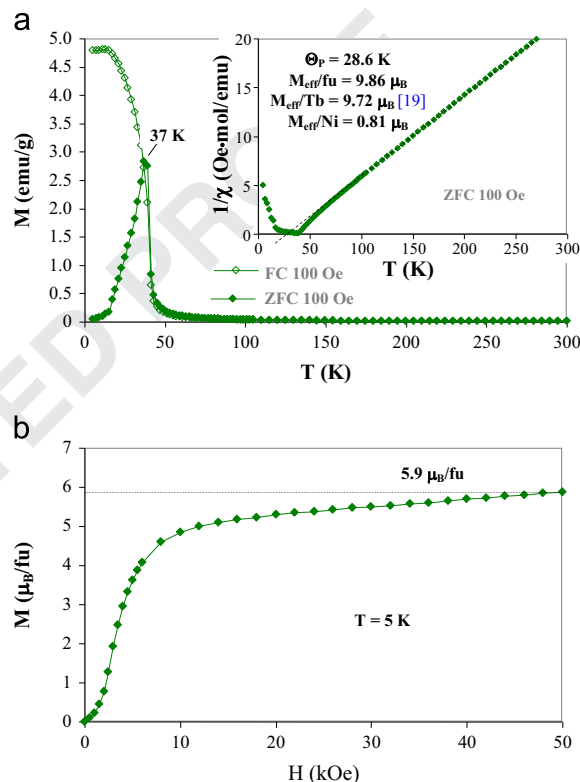


Fig. 1. (a) Magnetization and inverse magnetic susceptibility as a function of temperature, (b) magnetization vs. magnetic field at 5 K of TbNi₄Si.

Table 1
Atomic positions for the 2a, 4i and 4f sites of the *Cmmm*^a space group (retained by TbNi₄Si) with the corresponding symmetry operators and magnetic space group *Cmm'm*^b (retained by b-axis collinear ferromagnetic ordering of TbNi₄Si) with corresponding magnetic symmetry operators.

Site	Atom	x/a	y/b	z/c	Symmetry operator	Magnetic symmetry operator
2a	Tb ¹	0	0	0	<i>Pmmm</i> ^c	<i>Pmm'm</i> ^f
	Tb ²	1/2	1/2	1/2	<i>Pmmm</i> /[1/2 0 1/2]	<i>Pmm'm</i> × 1/[1/2 0 1/2]
4i	Ni1 ¹	0	y	0	<i>Pm2m</i> ^d	<i>Pm2m</i> ^g
	Ni1 ²	0	−y	0	{ <i>2</i> _x , <i>m</i> _y , <i>2</i> _z , <i>T</i> }	1' × { <i>2</i> _x , <i>m</i> _y , <i>2</i> _z , <i>T</i> }
	Ni1 ³	1/2	1/2 + y	0	<i>Pm2m</i> /[1/2 1/2 0]	<i>Pm2m</i> × 1/[1/2 1/2 0]
	Ni1 ⁴	1/2	1/2 − y	0	{ <i>2</i> _x , <i>m</i> _y , <i>2</i> _z , <i>T</i> }/[1/2 1/2 0]	1' × { <i>2</i> _x , <i>m</i> _y , <i>2</i> _z , <i>T</i> }/[1/2 1/2 0]
4f	Ni2 ¹	1/4	1/4	1/2	<i>P2₁/n</i> ^e	<i>P2₁/n</i> ^h
	Ni2 ²	−1/4	1/4	1/2	{ <i>m</i> _x , <i>2</i> _x /[1/2 1/2 0], <i>2</i> _y , <i>m</i> _y /[1/2 1/2 0]}	{ <i>m</i> _x , 1' × <i>2</i> _x /[1/2 1/2 0], <i>2</i> _y , 1' × <i>m</i> _y /[1/2 1/2 0]}
	Ni2 ³	1/4	−1/4	1/2	{ <i>m</i> _x /[1/2 1/2 0], <i>2</i> _x , <i>2</i> _y /[1/2 1/2 0], <i>m</i> _y }	{ <i>m</i> _x /[1/2 1/2 0], 1' × <i>2</i> _x , <i>2</i> _y /[1/2 1/2 0], 1' × <i>m</i> _y }
	Ni2 ⁴	−1/4	−1/4	1/2	<i>P2₁/n</i> /[1/2 1/2 0]	<i>P2₁/n</i> /[1/2 1/2 0]

^a *Cmmm* = {1, *m*_x, *m*_y, *m*_z, *T*, *2*_x, *2*_y, *2*_z} × {1, 1/[1/2, 1/2, 0]} = *Pmmm* × {1, 1/[1/2, 1/2, 0]};

^b *Cmm'm* = {1, *m*_x, 1' × *m*_y, *m*_z, 1' × *T*, 1' × *2*_x, *2*_y, 1' × *2*_z} × {1, 1/[1/2, 1/2, 0]} = {1, *m*_x, *2*_y, *m*_z} × {1, 1' × *T*} × {1, 1/[1/2, 1/2, 0]} = *Pmm'm* × {1, 1/[1/2, 1/2, 0]};

^c *Pmmm* = {1, *m*_x, *m*_y, *m*_z, *T*, *2*_x, *2*_y, *2*_z};

^d *Pm2m* = {1, *m*_x, *2*_y, *m*_z};

^e *P2₁/n* = {1, *m*_z, *2*_x/[1/2 1/2 0], *T*/[1/2 1/2 0]};

^f *Pmm'm* = {1, *m*_x, 1' × *m*_y, *m*_z, 1' × *T*, 1' × *2*_x, *2*_y, 1' × *2*_z} = *Pm2m* × {1, 1' × *m*_y};

^g *Pm2m* = *Pm2m* = {1, *m*_x, *2*_y, *m*_z}; and

^h *P2₁/n* = {1, *m*_z, 1' × *2*_x/[1/2 1/2 0], 1' × *T*/[1/2 1/2 0]} = {1, *m*_z} × {1, 1' × *2*_x/[1/2 1/2 0]}.

interactions, which can be easily overcome in small magnetic fields. The paramagnetic susceptibility of TbNi₄Si follows the Curie-Weiss law in the temperature range 90–300 K (inset in Fig. 1a). The fit to the Curie-Weiss law yields a positive paramagnetic Weiss temperatures $\theta_p = 28.6$ K and the effective moment per formula unit ($M_{\text{eff}}/\text{f.u.}$) of $9.86 \mu_B$. If Tb atoms are assumed to carry the theoretical Tb³⁺ effective moment of $\mu_{\text{eff}} = g[J(J+1)]^{1/2} \mu_B = 9.72 \mu_B$ [19], Ni atoms will have an effective paramagnetic magnetic moment of $0.81 \mu_B$ in TbNi₄Si. Such magnetic moment is little more than the theoretical magnetic moment of elemental Ni ($0.616 \mu_B$) [19]. However the neutron diffraction studies do not confirm presence of magnetic moments on Ni, and thus only Tb atoms are assumed to carry localized magnetic moments. In this case, the effective magnetic moment of the Tb atoms is $9.86 \mu_B$, and a slight increase of $\sim 0.14 \mu_B$ over the theoretical value can be attributed to the polarization of conduction electrons, predominantly the Tb 5d ones, through the 4f–5d exchange interactions.

The magnetization vs. magnetic field for TbNi₄Si at 5 K is plotted in Fig. 1b. A rapid increase in the magnetization at low fields is typical for a ferromagnet and is attributed to the domain growth. However, a subsequent slow linear increase and non-saturating behavior is indicative of the competing antiferromagnetic interactions and/or strong anisotropy. Based on the temperature-dependent magnetization data, the antiferromagnetic interactions are weak and easily overcome at fields of 100 Oe. Thus, a strong magnetic anisotropy is likely to be present in the TbNi₄Si structure and does not allow the magnetic moments to be fully oriented in the magnetic field. The saturation magnetic moment reaches the value of $5.9 \mu_B/\text{Tb}$ in 50 kOe, which is significantly smaller than the theoretical saturation moment of Tb³⁺ ($\mu = gJ \mu_B = 9 \mu_B$ [19]).

The magnetocaloric effect of TbNi₄Si in terms of the isothermal magnetic entropy change, ΔS_{mag} , was calculated from the

saturation magnetization data (Fig. 2a). A numerical integration is performed using the following formula $\Delta S(T)_{\text{mag}} = \sum_i (M_{i+1} - M_i/T_{i+1} - T_i) \Delta H$, where ΔH is a magnetic field step and M_i and M_{i+1} are the values of magnetization at temperatures T_i and T_{i+1} , respectively [14]. The magnetic entropy change, ΔS_{mag} , for $\Delta H = 0 - 5$ kOe is plotted in Fig. 2b. As expected for a second order magnetic transition, ΔS_{mag} peaks around the Curie temperature and has a maximum value of -6.3 J/kg K.

4.3. Magnetic structure

Above 38 K, the neutron diffraction patterns of TbNi₄Si in a zero applied field correspond to the paramagnetic state, and at

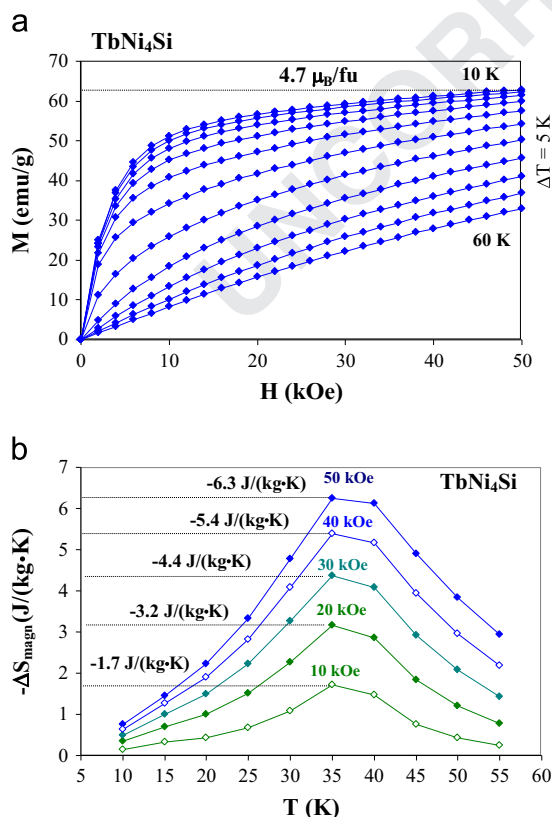


Fig. 2. (a) Magnetization vs. magnetic field and (b) the isothermal entropy change, $-\Delta S_{\text{mag}}$, of TbNi₄Si around the magnetic transitions.

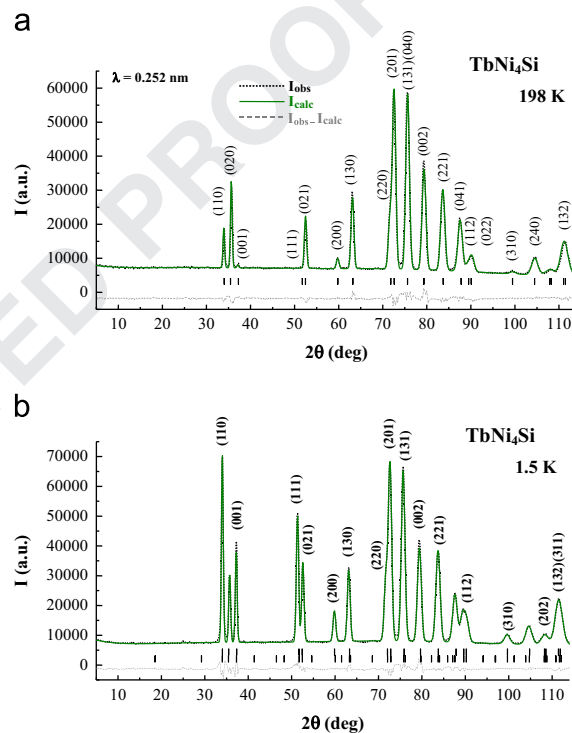


Fig. 3. Neutron diffraction patterns of TbNi₄Si (a) at 198 K (paramagnetic state) and (b) at 1.5 K (b -axis ferromagnet with $\mathbf{K}=[0, 0, 0]$ wave vector). The first row of ticks refers to the nuclear Bragg peaks whereas the second row of lines refers to the magnetic reflections. The (hkl) of strongest magnetic reflections are indicated in (b).

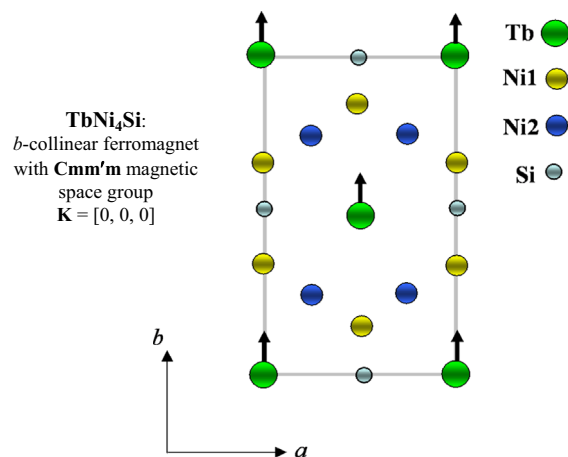


Fig. 4. The image of magnetic structure of YNi₄Si-type TbNi₄Si with b -axis collinear ferromagnetic ordering of Tb sublattice below ~ 38 K of $\text{Cmm}'\text{m}$ magnetic space group ($\mathbf{K}=[0, 0, 0]$ wave vector).

$T_C^{ND} = 38$ K a set of commensurate magnetic reflections with a $\mathbf{K} = [0, 0, 0]$ wave vector indicates the magnetic ordering of TbNi₄Si (Fig. 3). The ordering temperature found from the neutron diffraction study is in good agreement with the value deduced from the magnetization measurements of $T_C \sim 37$ K.

A commensurate b -axis collinear ferromagnetic model of TbNi₄Si fits best with the NDP data (Fig. 4).

Within this model, the calculated magnetic moments for the Ni1 and Ni2 sublattices are close to or within the error bar ($M_{Ni} \sim 0.12(12 \mu_B)$) meaning that the significance of such ordered magnetic moment on Ni cannot be confirmed. The other tested commensurate variants yielded no magnetic ordering for the Ni sublattices. The b -collinear magnetic ordering of the Tb sublattice corresponds to the $Cmm'm$ magnetic space group as shown in Table 1. The terbium magnetic moment reaches $8.66(6) \mu_B$ at 1.5 K, a value close to the theoretical value of $9 \mu_B$ expected for Tb magnetic moment [19] (Fig. 5 and Table 2).

The temperature-dependant changes in the lattice parameters are presented in Fig. 6. The unit cell of TbNi₄Si undergoes anisotropic distortion down to temperature of ferromagnetic transition, the cell parameters decrease with $a_T/a_{298 K} < c_T/c_{298 K} < b_T/b_{298 K}$; whereas $b/3^{1/2} \cdot a$ increases and below ferromagnetic ordering the cell parameters remain almost constant. As the TbNi₄Si structure is an orthorhombically distorted variant of the hexagonal CaCu₅ structure, the $b/3^{1/2} \cdot a$ ratio can be used to estimate the degree of the distortion and its progression with temperature. The $b/3^{1/2} \cdot a$ ratio increases upon cooling from 0.93755(3) at 298 K up to 0.93832(8) at 36 K and it stays almost constant below the Curie

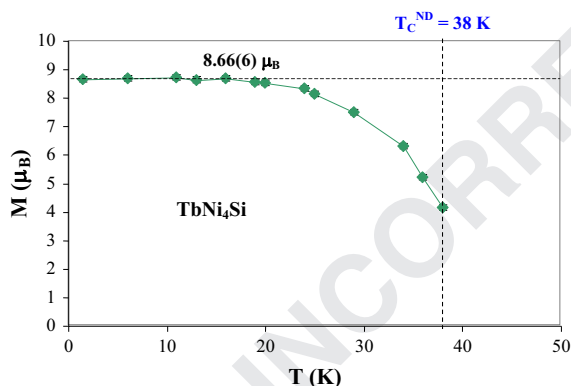


Fig. 5. The thermal evolution of Tb magnetic moment in the TbNi₄Si compound from the ND data.

Table 2

Crystallographic and magnetic parameters of YNi₄Si-type TbNi₄Si at different temperatures: cell parameters a , b and c , unit cell volume V , $b/(3^{1/2} \cdot a)$ ratio, the atomic position of Ni1 atom y_{Ni1} , $M_b^{K_0}$ the magnetic moments of Tb, Ni1 and Ni2 along the b -axis with $\mathbf{K}_0 = [0, 0, 0]$ wave vector. Reliability factors are: R_F for the crystal structure and R_F^m for the magnetic structure.

T (K)	Cell parameters (nm)	V (nm ³)	$b/(3^{1/2} \cdot a)$	y_{Ni1}	R_F (%)	Atom	$M_b^{K_0}$ (μ_B)	R_F^m (%)
298 ^b	$a = 0.50577(2)$ $b = 0.82131(3)$ $c = 0.39484(1)$	0.16401(4)	0.93755(3)	0.3453(5)	4.9			
198	$a = 0.50543(3)$ $b = 0.82090(6)$ $c = 0.39458(2)$	0.16371(8)	0.93771(7)	0.3407(2)	3.9			
1.5	$a = 0.50481(4)$ $b = 0.82048(6)$ $c = 0.39422(2)$	0.16328(8)	0.93838(7)	0.3403(3)	2.9	Tb ¹ , Tb ²	8.66(6)	3.3

^a Atomic sites of YNi₄Si-type TbNi₄Si (space group $Cmmm$): Tb1 (2a) [0, 0, 0], Ni1 (4i) [0, 0.3453(5), 0], Ni2 (4f) [1/4, 1/4, 1/2] and Si (2c) [0, 1/2, 1/2].

^b X-ray data.

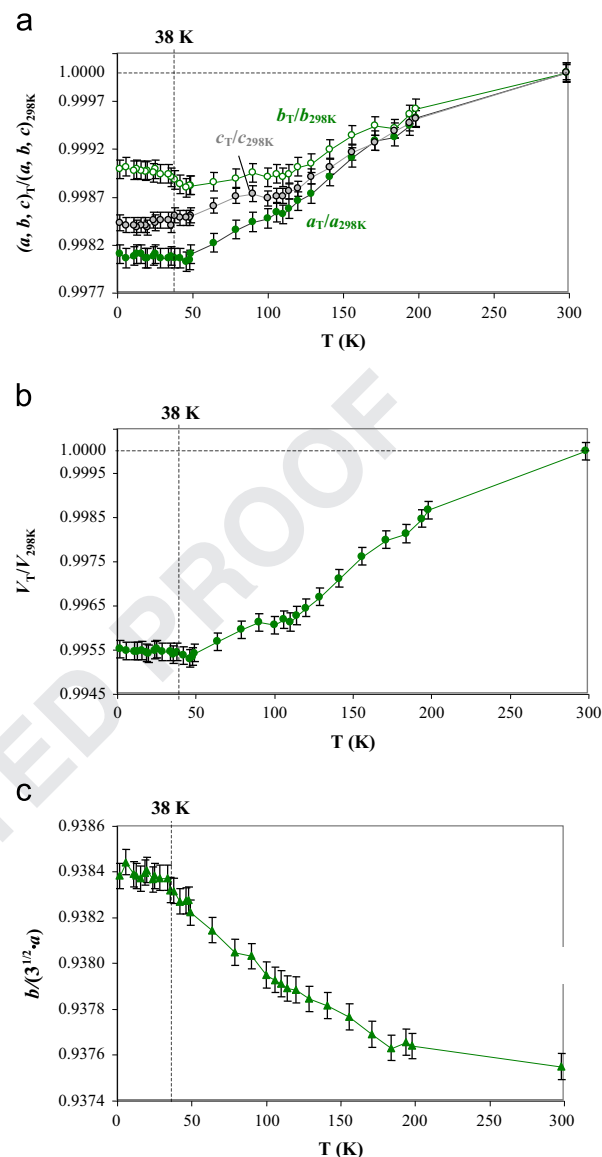


Fig. 6. Thermal variation of relative cell parameters (a) $a_T/a_{298 K}$, $b_T/b_{298 K}$ and $c_T/c_{298 K}$, (b) $V_T/V_{298 K}$ and (c) $b/(3^{1/2} \cdot a)$. Here a_T , b_T , c_T , V_T , $a_{298 K}$, $b_{298 K}$, $c_{298 K}$ and $V_{298 K}$ are cell parameters and unit cell volume of TbNi₄Si at temperature T and at 298 K, respectively. The $b/3^{1/2} \cdot a$ ratio is the degree of the distortion of initial CaCu₅-type lattice.

temperature ($b/3^{1/2} \cdot a = 0.92838(7)$) at 1.5 K). The obtained value of $b/3^{1/2} \cdot a$ ratio too far from the value 1 that corresponds to the transformation of orthorhombic YNi_4Si -type lattice in to hexagonal CaCu_5 -type lattice.

5. Discussion

The saturation magnetization at 5 K and in 50 kOe yielded a magnetic moment of $5.9 \mu_B$ per terbium atom (Fig. 1b);, whereas neutron diffraction studies at 1.5 K and in a zero applied field indicated a complete ferromagnetic ordering of TbNi_4Si with $8.66 \mu_B/\text{Tb}$ (Fig. 5). Most likely, a large magnetic anisotropy prevents a parallel alignment of all the Tb moments in the polycrystalline sample with the magnetic field even at 50 kOe.

Thus, we cannot unambiguously claim for the influence the orthorhombic distortion for magnetocaloric effect of TbNi_5 . Meanwhile, orthorhombic distortion of unit cell (compression of unit cell along the b -orthorhombic axis) leads to the change in the Tb environment: Tb–Tb 0.3966 nm and Tb–6Tb 0.4894 nm of TbNi_5 transform in to Tb–Tb2 0.39484 nm, Tb–4Tb 0.48227 nm and Tb–Tb2 0.50577 nm of TbNi_4Si (the interatomic distances are given at 298 K). This distortion of unit cell leads to the disappearance of the incommensurate component in the initial TbNi_5 magnetic structure, increasing of temperature of magnetic ordering from 24 K up to 37 K and reorientation the terbium moments in the ab -plane normal to the compression of unit cell.

Thus from present experimental data the orthorhombic distortion of initial CaCu_5 -type unit cell of TbNi_5 leads to the suppression of the incommensurate magnetic component, increase of Curie temperature and a decrease of magnetocaloric effect in YNi_4Si -type TbNi_4Si .

6. Conclusions

This work suggests possible existence of other YNi_4Si -type solid solutions with such orthorhombic distortion of initial CaCu_5 -type unit cell. Perhaps, the orthorhombic distortion of initial CaCu_5 -type compounds is a prospective route for optimization of their magnetic and hydrogen storage properties.

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